

REG-PROB-2425-ASM-SET 4-MATH

建議題解

結構式試題

1. (a) 所求概率 = $\frac{C_2^3}{C_2^5}$ 1M
 $= \frac{3}{10}$ 1A
 (b) 所求概率 = $\frac{C_1^3 \times C_1^2}{C_2^5}$ 1M
 $= \frac{3}{5}$ 1A
 (c) 所求概率 = $\frac{3}{10} \times \frac{2}{4} + \frac{3}{5} \times \frac{1}{4} + \left(1 - \frac{3}{10} - \frac{3}{5}\right) \times 0$ 1M+1A
 $= \frac{3}{10}$ 1A
2. (a) 所求概率 = $\frac{C_3^{20} C_2^{15}}{C_5^{35}}$ 1M
 $= \frac{4275}{11\,594}$ 1A
 (b) 所求概率 = $\frac{C_3^{20} C_2^{10}}{C_3^{20} C_2^{15} + C_4^{20} C_1^{15} + C_5^{20}}$ 1M
 $= \frac{900}{3647}$ 1A
3. (a) 所求概率 = $\frac{C_4^8 C_2^6 + C_5^8 C_1^6 + C_6^8}{C_6^{8+6}}$ 1M
 $= \frac{202}{429}$ 1A
 (b) 所求概率 = $\frac{C_3^7 C_2^5 + C_4^7 C_1^5}{C_4^8 C_2^6}$ 1M
 $= \frac{1}{2}$ 1A
4. (a) 所求概率 = $1 - \frac{C_2^5}{C_2^9}$ 1M
 $= \frac{13}{18}$ 1A
 (b) 所求概率 = $\frac{\left(\frac{C_2^4}{C_2^9}\right)}{\left(\frac{13}{18}\right)}$ 1M
 $= \frac{3}{13}$ 1A

5. (a) 所求概率 = $\frac{1}{2} \cdot \frac{C_1^4 C_2^8}{C_3^{12}} + \frac{1}{2} \cdot \frac{C_1^2 C_2^8}{C_3^{10}}$ 1M+1A
 $= \frac{161}{330}$ 1A
- (b) 所求概率 = $\frac{\frac{1}{2} \cdot \frac{C_1^4 C_2^8}{C_3^{12}}}{\frac{161}{330}}$ 1M
 $= \frac{12}{23}$ 1A
6. (a) 方法數目 = $C_{10}^{8+7} = 3003$ 1A
- (b) 所求概率 = $\frac{C_5^7 C_5^8 + C_6^7 C_4^8 + C_7^7 C_3^8}{C_{10}^{15}}$ 1M
 $= \frac{82}{143}$ 1A
- (c) 所求概率 = $\frac{\frac{C_6^7 C_4^8}{C_{10}^{15}}}{\frac{82}{143}}$ 1M
 $= \frac{35}{123}$ 1A
7. (a) 方法數目 = C_4^{10} 1M
 $= 210$ 1A
- (b) 所求概率 = $\frac{C_4^8}{C_4^8 + C_2^8}$ 1M+1A
 $= \frac{5}{7}$ 1A
8. (a) 所求概率 = $1 - \frac{C_6^{14} + C_6^{16}}{C_6^{30}}$ 1M+1A
 $= \frac{6404}{6525}$ 1A
- (b) 所求概率 = $\frac{\frac{C_2^{14} C_4^{16} + C_1^{14} C_5^{16}}{C_6^{30}}}{\frac{6404}{6525}}$ 1M+1M
 $= \frac{623}{1601}$ 1A
9. (a) 所求概率 = $1 - \frac{C_3^{10} C_3^6}{C_6^{16}}$ 1M
 $= \frac{701}{1001}$ 1A

$$\begin{aligned}
 \text{(b) 所求概率} &= 1 - \frac{C_6^{10} + C_5^{10} C_1^6}{C_6^{16}} && 1M \\
 &= \frac{449}{572} && 1A \\
 \text{(c) 所求概率} &= \frac{C_3^{10} C_3^6 + C_4^{10} C_2^6}{C_6^{16}} \div \frac{449}{572} && 1M+1A \\
 &= \frac{2775}{3143} && 1A
 \end{aligned}$$

10. (a) 男老師的數目 = 30；女老師的數目 = 20。

$$\begin{aligned}
 \text{所求概率} &= \frac{C_2^{30} + C_2^{20}}{C_2^{50}} && 1M \\
 &= \frac{25}{49} && 1A
 \end{aligned}$$

(b) 接受過專業訓練的男老師的數目 = 24

接受過專業訓練的女老師的數目 = 14

$$\begin{aligned}
 \text{所求概率} &= \frac{24 \times 14}{C_2^{50}} && 1M \\
 &= \frac{48}{175} && 1A
 \end{aligned}$$

$$\begin{aligned}
 \text{(c) 所求概率} &= \frac{\left(\frac{6 \times 6}{C_2^{50}}\right)}{\left(\frac{C_2^{12}}{C_2^{50}}\right)} && 1M+1A \\
 &= \frac{6}{11} && 1A
 \end{aligned}$$

11. (a) 所求概率 = $0.2 \times 0.35 + 0.5 \times 0.55 + 0.3 \times 0.25$

$$= 0.42 \quad 1M$$

(b) (i) 所求概率 = $0.2^3 + 0.5^3 + 0.3^3$

$$= 0.16 \quad 1M$$

$$\begin{aligned}
 \text{(ii) 所求概率} &= \frac{(0.2 \times 0.35)^3 + (0.5 \times 0.55)^3 + (0.3 \times 0.25)^3}{0.16} && 1M+1A \\
 &\approx 0.135 && 1A
 \end{aligned}$$

$$\begin{aligned}
 \text{(iii) 所求概率} &= \frac{(0.2 \times 0.35)^3}{0.42^3} && 1M \\
 &\approx 0.00463 && 1A
 \end{aligned}$$