

REG-LOCUS-2425-ASM-SET 1-MATH**Suggested solutions****Multiple Choice Questions**

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|-------|-------|-------|-------|-------|
| 1. D | 2. A | 3. A | 4. D | 5. B |
| 6. D | 7. B | 8. B | 9. C | 10. C |
| 11. B | 12. C | 13. D | 14. D | 15. A |
| 16. A | 17. A | 18. D | 19. A | 20. C |
| 21. A | 22. D | 23. A | 24. A | |

1. ☐ D

L_1 and L_2 are not parallel lines.

The locus of P is the angle bisectors of the angles formed by L_1 and L_2 , which is a pair of perpendicular lines.

2. ☐ A

Locus of P is a circle with diameter AB .

3. ☐ A

Fixed distance to a fixed point \Rightarrow circle

4. ☐ D

L_1 and L_2 are parallel.

Required locus is a straight line parallel to L_1 , and is in the middle of L_1 and L_2 .

5. ☐ B

AB and BC are not parallel. The locus of P is the angle bisector of $\angle ABC$.

I. ✗. The locus is not perpendicular to AC unless $AB = BC$.

II. ✗. The locus does not pass through the mid-point of AC unless $AB = BC$.

III. ✓.

6. ☐ D

Locus of P is a pair of straight lines parallel to L .

7. ☐ B

The locus of P is the angle bisectors of the angles formed by the x -axis and y -axis.

The answer is B.

8. B

Distance from P to the line AB is the height of $\triangle PAB$, which is a constant.
The locus of P is a pair of straight lines, with a fixed distance to the line AB .

9. C

The locus of P is a pair of straight lines, $y = -1$ and $y = 11$.

10. C

The locus of P is the angle bisector of $\angle AOF$.

$\angle AOF = 40^\circ + 30^\circ \times 2 + 10^\circ + 50^\circ = 160^\circ$
Note that $\angle AOD = 40^\circ + 30^\circ + 10^\circ = 80^\circ = \frac{160^\circ}{2}$.
The locus of P is the line segment OD .

11. B

The locus of P passes through B , J and D . It is the line segment BD .

12. C

The locus of P is the angle bisectors of the angles formed by the two intersecting lines.
The two angle bisectors are perpendicular to each other.

13. D

Let M and N be the mid-points of AB and CD respectively.

I. The locus is the perpendicular bisector of AB .

It is the line segment MN .

II. The locus is the straight line parallel to AD and passes through the mid-point of AB .

It is the line segment MN .

III. Note that $\triangle PCD$ is isosceles. P is equidistant from C and D .

The locus of P is the perpendicular bisector of CD .

It is the line segment MN .

Three conditions will all give the same locus of P .

14. D

The locus of Q passes through F , J and H . It is the line segment FH .

15. A

Equidistant from two fixed points \Rightarrow perpendicular bisector

16. A

P maintains a fixed distance to point A . So, the locus of P is a circle.

17. A

Let $P(x, y)$.

Then the coordinates of A and B are $(2x, 0)$ and $(0, 2y)$ respectively.

$$AB = \sqrt{(2x)^2 + (2y)^2}$$

$$x^2 + y^2 = \frac{(AB)^2}{4}$$

Locus of P is a arc (part of circle) with centre $(0, 0)$ and radius $\frac{AB}{2}$.

18. D

Locus of P is the angle bisectors of the angles between L_1 and L_2 .

Locus of P is therefore a pair of straight lines (perpendicular to each other, passing through intersection of L_1 and L_2).

19. A

Locus of P is the perpendicular bisector of AB , i.e., a straight line.

20. C

Let $P = (x, y)$.

$$PX = 2PY$$

$$\sqrt{x^2 + (y - 5)^2} = 2\sqrt{(x - 1)^2 + y^2}$$

$$x^2 + (y - 5)^2 = 4[(x - 1)^2 + y^2]$$

$$0 = 3x^2 + 3y^2 - 8x + 10y - 21$$

21. A

The locus of P is a circle with centre $A(2, -5)$ and radius AB .

A. ✓. Centre $(2, -5)$ and $8^2 + 3^2 - 4(8) + 10(3) - 71 = 0$.

B. ✗. Centre $(-2, 5)$

C. ✗. Centre $(-2, 5)$

D. ✗. Centre $(2, -5)$ but $8^2 + 3^2 - 4(8) + 10(3) - 75 = -4 \neq 0$.

22. D

Let the coordinates of P be (x, y) .

$$\frac{y - 4}{x - 0} \times \frac{y - 2}{x - 6} = -1$$

$$(y - 4)(y - 2) = -x(x - 6)$$

$$x^2 + y^2 - 6x - 6y + 8 = 0$$

Required equation is $x^2 + y^2 - 6x - 6y + 8 = 0$.

23. A

It is the perpendicular bisector of AB .

Slope of $AB = \frac{5+1}{1+5} = 1$. Slope of locus $= -1$. Only option A has a line with slope -1 .

24. A

The coordinates of A and B are $(5, 0)$ and $(0, -12)$ respectively.

The locus of P is the perpendicular bisector of AB .

The coordinates of mid-point of AB are $\left(\frac{5}{2}, -6\right)$.

Note that $15x + 36y + 179 = 15\left(\frac{5}{2}\right) + 36(-6) + 179$ is not an integer, implying it cannot be zero.

The answer is A.

Conventional Questions

25. (a) Let the coordinates of P be (x, y) .

$$[(x-8)^2 + (y-1)^2] + [(x-3)^2 + (y-4)^2] = (8-3)^2 + (4-1)^2 \quad 1M$$

$$2x^2 + 2y^2 - 22x - 10y + 56 = 0$$

$$x^2 + y^2 - 11x - 5y + 28 = 0$$

The equation of the locus of P is $x^2 + y^2 - 11x - 5y + 28 = 0$. 1A

- (b) Let the coordinates of P be (x, y) .

$$[(8-3)^2 + (4-1)^2] + [(x-3)^2 + (y-4)^2] = (x-8)^2 + (y-1)^2 \quad 1M$$

$$10x - 6y - 6 = 0$$

$$5x - 3y - 3 = 0$$

The equation of the locus of P is $5x - 3y - 3 = 0$. 1A

- (c) Let the coordinates of P be (x, y) .

$$\sqrt{(x-8)^2 + (y-1)^2} = \sqrt{(x-3)^2 + (y-4)^2} \quad 1M$$

$$-10x + 6y = 40$$

$$5x - 3y - 20 = 0$$

The equation of the locus of P is $5x - 3y - 20 = 0$. 1A

26. (a) Let the coordinates of P be (x, y) . Then the coordinates of F are $(x, 3)$.

$$[(x-2)^2 + y^2] + [x^2 + (y+2)^2] = 2(y-3)^2 \quad 1M$$

$$2x^2 + 2y^2 - 4x + 4y + 8 = 2y^2 - 12y + 18$$

$$y = -\frac{x^2}{8} + \frac{x}{4} + \frac{5}{8}$$

The equation of the locus of P is $y = -\frac{x^2}{8} + \frac{x}{4} + \frac{5}{8}$. 1A

- (b) The locus of P is a parabola that opens downwards. 1A

27. (a) Length of $AB = 4$. Distance from P to $AB = \frac{6 \times 2}{4} = 3$ 1A

The locus of P is a pair of vertical straight lines 3 units on the left and right of AB respectively.

1A

- (b) The equations of the locus of P are $x = -1$ and $x = 5$. 1M+1A

28. (a) Let the coordinates of B be (p, q) .

$$\frac{q-4}{p-0} \times (-1) = -1 \quad 1M$$

$$q - 4 = p$$

mid-point of AB is at $\left(\frac{p}{2}, \frac{q+4}{2}\right)$.

$$\text{So, } \frac{q+4}{2} = -\frac{p}{2}. \quad 1\text{M}$$

Solving, we have $p = -4$ and $q = 0$. The coordinates of B are $(-4, 0)$. 1A

$$(b) \quad \frac{y-4}{x-0} \times \frac{y-0}{x+4} = -1 \quad 1\text{M}$$

$$y(y-4) + x(x+4) = 0$$

$$x^2 + y^2 + 4x - 4y = 0 \quad 1$$

$$(c) \text{ Radius of } \Gamma = \sqrt{2^2 + 2^2} = 2\sqrt{2}$$

$$\pi r^2 - \pi(2\sqrt{2})^2 = \pi(2\sqrt{2})^2 \quad 1\text{M}$$

$$r^2 = 16$$

$$r = 4 \quad 1\text{A}$$