

## REG-EOC-2425-ASM-SET 6-MATH

### Suggested solutions

#### Multiple Choice Questions

1. B	2. C	3. C	4. D	5. B
6. A	7. B	8. C	9. A	10. C
11. D	12. D	13. A	14. D	15. A
16. A	17. A	18. A	19. B	20. D

1. B

Solve  $\begin{cases} 2x - y = 25 \\ x^2 + y^2 - 52x - 34y + 925 = 0 \end{cases}$ , we have  $(x, y) = (24, 23)$  or  $(20, 15)$ .

The coordinates of  $P$  and  $Q$  are  $(24, 23)$  and  $(20, 15)$ .

The coordinates of the mid-point of  $PQ$  are  $(22, 19)$ .

Required equation is

$$(x - 22)^2 + (y - 19)^2 = (20 - 22)^2 + (15 - 19)^2$$
$$(x - 22)^2 + (y - 19)^2 = 20$$

2. C

Use the calculator program to check the intersections.

- A. ✗. Centre of this circle is at  $(-3, 1)$ .
- B. ✗. MATH ERROR  $\Rightarrow$  no intersections.
- C. ✓. Only one intersection  $\Rightarrow$  circle touches the line.
- D. ✗. MATH ERROR  $\Rightarrow$  no intersections.

3. C

Solve the system  $\begin{cases} 3x + 4y - k = 0 \\ x^2 + y^2 - 4x - 2y - 20 = 0 \end{cases}$  using the calculator program.

The system has repeated solutions when  $k = 35$  or  $-15$ .

Thus,  $k = 35$  or  $-15$ .

4. D

Solve the system  $\begin{cases} mx - y - 1 = 0 \\ x^2 + y^2 - 16x - 2y + 31 = 0 \end{cases}$  using the calculator program.

The system has repeated solutions when  $m = \frac{5}{3}$  and when  $m = -\frac{3}{5}$ .

Thus,  $m = \frac{5}{3}$  or  $-\frac{3}{5}$ .

5. **B**

Solve the system  $\begin{cases} x + 2y - 5 = 0 \\ x^2 + y^2 + 2kx - 4y + k^2 - 1 = 0 \end{cases}$  using the calculator program.

The system has repeated solutions when  $k = -6$  or  $4$ .

The coordinates of the centre are  $(-4, 2)$  or  $(6, 2)$ .

6. **A**

Solve the system  $\begin{cases} x + y + k = 0 \\ x^2 + y^2 - 6x - 2y + 8 = 0 \end{cases}$  using the calculator program.

The system has repeated solutions when  $k = -2$  or  $-6$ .

Thus,  $k = -2$  or  $-6$ .

7. **B**

Solve the system  $\begin{cases} kx + y = 0 \\ x^2 + y^2 - 2x - y + 1 = 0 \end{cases}$  using the calculator program.

Value of $k$	Number of intersections	Sign of $\Delta$
$-\frac{4}{3}$	1	
1	0	-

$-\frac{4}{3}$  is a boundary value of the required range.

Required range does not contain 1.

The answer is B.

8. **C**

Solve the simultaneous equations  $\begin{cases} mx - y - 5 = 0 \\ x^2 + y^2 - 11x + 7y + 20 = 0 \end{cases}$  using the calculator program.

Value of $m$	Number of intersections	Sign of $\Delta$
-3	0	-

Required range contains  $-3$  and  $-3$  is not a boundary value.

The answer is C.

9. **A**

Solve the system  $\begin{cases} x - 2y + k = 0 \\ x^2 + y^2 - 12x - 24y - 320 = 0 \end{cases}$  using the calculator program.

Value of $k$	Number of intersections	Sign of $\Delta$
-32	1	

-32 is a boundary value of the required range.

The answer is A.

10. **C**

Solve the system  $\begin{cases} 5x + 3y + k = 0 \\ x^2 + y^2 - 6x + 10y = 0 \end{cases}$  using the calculator program.

Value of $k$	Number of intersections	Sign of $\Delta$
-17	2	+

-17 is not a boundary value of the required range.

Required range contains -17.

The answer is C.

11. **D**

Solve the system  $\begin{cases} x + ky - 3 = 0 \\ x^2 + y^2 - 4x - 6y + 5 = 0 \end{cases}$  using the calculator program.

Value of $k$	Number of intersection	Sign of $\Delta$
-7	0	-

-7 is not a boundary value of the required range.

Required range contains -7.

The answer is D.

12. **D**

Solve the system  $\begin{cases} x - y + m = 0 \\ x^2 + y^2 + 2x - 4y - 13 = 0 \end{cases}$  using the calculator program.

Value of $m$	Number of intersections	Sign of $\Delta$
-9	0	-

Required range does not contain  $m = -9$  and -9 is not a boundary value of the required range.

The answer is D.

13. **A**

Solve the system  $\begin{cases} kx - y + 2 = 0 \\ x^2 + y^2 - 5x - 9y + 24 = 0 \end{cases}$  using calculator program.

Value of $k$	Number of intersection	Sign of $\Delta$
$\frac{1}{3}$	1	0
-3	0	-

Required range has  $\frac{1}{3}$  as one of the boundary value, and it contains  $k = -3$ .

The answer is A.

14. **D**

Solve the system  $\begin{cases} kx - y - 3 = 0 \\ x^2 + y^2 + 4x + 8y + 19 = 0 \end{cases}$  using the calculator program.

Value of $k$	Number of intersection	Sign of $\Delta$
$-\frac{3}{4}$	0	-
$\frac{3}{4}$	2	+

$-\frac{3}{4}$  and  $\frac{3}{4}$  are not boundary values of the required range.

Required range contains  $-\frac{3}{4}$ , while it does not contain  $\frac{3}{4}$ .

The answer is D.

15. **A**

Solve the system  $\begin{cases} x + y = 0 \\ x^2 + y^2 + 2kx + k^2 - 8 = 0 \end{cases}$  using the calculator program.

Value of $k$	Number of intersection	Sign of $\Delta$
0	2	+

Required range contains 0.

The answer is A.

16. A

The equation of  $L$  is  $y = -\frac{3x}{4} + k$ .

Solve the system  $\begin{cases} \frac{3x}{4} + y - k = 0 \\ x^2 + y^2 - 8x + 12y - 48 = 0 \end{cases}$  using the calculator program.

Value of $k$	Number of intersections	Sign of $\Delta$
0	2	+

Required range contains 0.

The answer is A.

17. A

Solve the system  $\begin{cases} 2x - y + k = 0 \\ x^2 + y^2 + 4x + ky + 3 = 0 \end{cases}$  using the calculator program.

Value of $k$	Number of intersection	Sign of $\Delta$
1	1	
0	0	-

1 is a boundary value of the required range.

Required range contains 0.

The answer is A.

18. A

Solve the system  $\begin{cases} 2x + y - 5 = 0 \\ x^2 + y^2 - kx + 6y - 10 = 0 \end{cases}$  using the calculator program.

Value of $k$	Number of intersections	Sign of $\Delta$
2	2	+

Required range does not contain 2 and 2 is not a boundary value of the range.

The answer is A.

19. **B**

Solve the system  $\begin{cases} mx - y - 2 = 0 \\ x^2 + y^2 + 6x + 5 = 0 \end{cases}$  using the calculator program.

Value of $m$	Number of intersection	Sign of $\Delta$
$\frac{12}{5}$	0	—

$\frac{12}{5}$  is not a boundary value of the required range.

Required range does not contain  $\frac{12}{5}$ .

The answer is B.

20. **D**

Solve the system  $\begin{cases} 2x + y + k = 0 \\ x^2 + y^2 + 12x - 8y + 32 = 0 \end{cases}$  using the calculator program.

Value of $k$	Number of intersection	Sign of $\Delta$
-18	0	—

-18 is not a boundary value of the required range.

Required range contains -18.

The answer is D.

### Conventional Questions

21.  $x^2 + (-2x - k)^2 + 2x + 2(-2x - k) - 3 = 0$  1M  
 $(1 + 4)x^2 + (4k + 2 - 4)x + (k^2 - 2k - 3) = 0$   
 $5x^2 + (4k - 2)x + (k^2 - 2k - 3) = 0$   
 $\Delta = (4k - 2)^2 - 4(5)(k^2 - 2k - 3) = 0$  1M  
 $(16 - 20)k^2 + (-16 + 40)k + (4 + 60) = 0$   
 $-4k^2 + 24k + 64 = 0$   
 $k = -2 \quad \text{or} \quad 8$  1A+1A

22.  $x^2 + (x + 9)^2 + 13x - 15(x + 9) + (4k + 6) = 0$  1M  
 $(1 + 1)x^2 + (18 + 13 - 15)x + (81 - 135 + 4k + 6) = 0$   
 $2x^2 + 16x + (4k - 48) = 0$   
 $\Delta = 16^2 - 4(2)(4k - 48) = 0$  1M  
 $-32k + 640 = 0$   
 $k = 20$  1A

23.  $x^2 + (3x + 8)^2 - 5x - 4(3x + 8) + k = 0$  1M  
 $(1 + 9)x^2 + (48 - 5 - 12)x + (64 - 32 + k) = 0$   
 $10x^2 + 31x + 32 + k = 0$  1A  
 $\Delta = 31^2 - 4(10)(32 + k) < 0$  1M  
 $-319 - 40k < 0$   
 $k > -\frac{319}{40}$   
Required value is  $-7$ . 1A

24.  $0^2 + y^2 + k(0) - 6y + 9 = 0$  1M  
 $y^2 - 6y + 9 = 0$   
 $(y - 3)^2 = 0$   
 $y = 3$  1M  
The circle intersect the  $y$ -axis at only one point.  
The circle touches the  $y$ -axis. 1