

REG-FG-2425-ASM-SET 2-MATH**Suggested solutions****Multiple Choice Questions**

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|-------|-------|-------|-------|-------|
| 1. A | 2. A | 3. B | 4. D | 5. A |
| 6. C | 7. C | 8. B | 9. C | 10. A |
| 11. C | 12. A | 13. D | 14. C | 15. B |
| 16. C | 17. B | 18. B | 19. D | 20. A |
| 21. D | 22. D | 23. D | 24. B | 25. B |
| 26. B | 27. D | 28. C | 29. A | 30. C |

1. ☐ A

The graph opens downwards when the coefficient of x^2 is negative.

The answer is A.

2. ☐ A

$$y = -2x^2 - 8x + 10 \rightarrow a = -2, b = -8 \text{ and } c = 10$$

Sign	Graph	Conclusion
$a < 0$	open downwards	B ✗ and D ✗
$b < 0$	slope at y-intercept is negative	C ✗

The answer is A.

3. ☐ B

Graph	Conclusion
Open upwards	$a > 0$
y-intercept is positive	$b > 0$

The answer is B.

4. ☐ D

Graph	Conclusion
Slope at y-intercept is negative	$p < 0$
y-intercept is negative	$q > 0$

The answer is D.

5. A

Consider the graph of $y = ax^2 + bx + c$.

Graph	Conclusion
Open upwards	$a > 0$
Slope at y-intercept is negative	$b < 0$
y-intercept is positive	$c > 0$

Consider the graph of $y = bx^2 + cx + a$.

Sign	Graph	Conclusion
$b < 0$	open downwards	C ✗ and D ✗
$c > 0$	slope at y-intercept is positive	B ✗

The answer is A.

6. C

$$y = x^2 - 6x + 6 \rightarrow a = 1, b = -6 \text{ and } c = 6$$

Sign	Graph	Conclusion
$a > 0$	open upwards	
$b < 0$	slope at y-intercept is negative	B ✗
$c > 0$	y-intercept is positive	

When $y = 0$,

$$0 = x^2 - 6x + 6$$

$$x \approx 4.73 \text{ or } 1.27$$

There are two x -intercepts.

The answer is C.

7. C

Graph	Conclusion
Open downwards	$m < 0$
y-intercept > 0	$n > 0$

The answer is C.

8. **B**

The graph opens downwards. We have $a < 0$.

The coordinates of the vertex of the graph are $(-b, c)$.

We have $-b < 0$ ($b > 0$) and $c > 0$.

Thus, $ab < 0$ and $c > 0$.

9. **C**

$$y = x^2 - 2x - 3 \rightarrow a = 1, b = -2 \text{ and } c = -3$$

Sign	Graph	Conclusion
$a > 0$	open upwards	A ✗ and B ✗
$b < 0$	slope at y-intercept is negative	D ✗
$c < 0$	y-intercept is negative	

The answer is C.

10. **A**

Slope at y-intercept = $b < 0$

When $y = 0$, the equation $-3x^2 + bx + c$ has no real roots.

$$\Delta = b^2 - 4(-3)(c) < 0$$

$$b^2 + 12c < 0$$

11. **C**

Graph	Conclusion
Open upwards	$m > 0$
y-intercept < 0	$n < 0$

The answer is C.

12. **A**

Graph	Conclusion
Open downwards	$a < 0$
y-intercept is positive	$c > 0$
Two x-intercepts	$\Delta = b^2 - 4ac > 0$

The answer is A.

13. D

The equation $x^2 - 16x + c$ has double real roots.

$$\Delta = 16^2 - 4(1)(c) = 0$$

$$c = 64$$

14. C

Coordinates of vertex are $(1, 1)$.

Vertex of the graph lies in the first quadrant.

The answer is C.

15. B

Coordinates of vertex are $(-h, k)$.

$$-h < 0 \quad \text{and} \quad k < 0$$

$$h > 0$$

The answer is B.

16. C

The coordinates of the vertex are $(-b, c)$.

We have $b = 0$ and $c < 0$.

17. B

I. ✗. Put $x = 0$, $y = 2(0 + a)^2 + b = 2a^2 + b$.

$$y\text{-intercept} = 2a^2 + b$$

II. ✓. The coordinates of the vertex are $(-a, b)$.

We have $-a > 0$ ($a < 0$) and $b < 0$.

Thus, $ab > 0$.

III. ✗.

18. B

$$y = (3x - 1)^2 - 9$$

$$= 9\left(x - \frac{1}{3}\right)^2 - 9$$

The coordinates of vertex are $\left(\frac{1}{3}, -9\right)$.

19. D

Coordinates of vertex are $(-1, 1)$.

Vertex of the graph lies in the second quadrant.

$$y\text{-intercept} = -2(0 + 1)^2 + 1$$

$$= -1 < 0$$

The answer is D.

20. A

$$\begin{aligned} \text{y-intercept} &= -(0 - 1)^2 + 9 \\ &= 8 \end{aligned}$$

21. D

$$\begin{aligned} \text{Vertex } (-b, 0) &\Rightarrow -b < 0 \Rightarrow b > 0 \\ \text{The graph opens upwards} &\Rightarrow a > 0 \end{aligned}$$

22. D

$$\begin{aligned} y &= (ax + 1)^2 + a \\ &= a^2 \left(x + \frac{1}{a} \right)^2 + a \end{aligned}$$

Coordinates of vertex are $\left(-\frac{1}{a}, a \right)$.

Since $-1 < a < 0$, vertex (\oplus, \ominus) lies in quadrant IV.

When $x = 0$, $y = 1 + a > 0 \Rightarrow$ y-intercept is positive.

23. D

$$\begin{aligned} y &= -(4x - 5)^2 + 8 \\ &= -16 \left(x - \frac{5}{4} \right)^2 + 8 \end{aligned}$$

The axis of symmetry is $x = \frac{5}{4}$.

24. B

When $x = 0$, $y = (0 + 2)^2 - 8 = -4$.

The coordinates of C are $(0, -4)$.

$$\begin{aligned} y &= (3x + 2)^2 - 8 \\ &= 9 \left(x + \frac{2}{3} \right)^2 - 8 \end{aligned}$$

The coordinates of A and B are $\left(-\frac{2}{3}, 0 \right)$ and $\left(-\frac{2}{3}, -8 \right)$ respectively.

$$\begin{aligned} \text{Required area} &= \frac{(4 + 8) \left(\frac{2}{3} \right)}{2} \\ &= 4 \end{aligned}$$

25. B

The coordinates of A are $(0, 7)$.

The coordinates of B are $(12, 7)$.

Consider the axis of symmetry.

$$h = \frac{0 + 12}{2}$$
$$= 6$$

Put $(0, 7)$ into $y = \frac{1}{2}(x - 6)^2 + k$.

$$7 = \frac{1}{2}(0 - 6)^2 + k$$

$$k = -11$$

26. B

We have $c = 5$.

Let the other x -intercept be β .

Then 1 and β are roots of $x^2 + bx + 5 = 0$.

$$\text{Product of roots} = 1\beta = \frac{5}{1}$$

$$\beta = 5$$

Equation of axis of symmetry is

$$x = \frac{1 + 5}{2}$$

$$x = 3$$

27. D

Using the x -intercepts, we have $f(x) = a(x + 2)(x - 3)$, where a is a constant.

Put $(0, 2)$ into $y = a(x + 2)(x - 3)$.

$$2 = a(0 + 2)(0 - 3)$$

$$a = -\frac{1}{3}$$

Thus, $f(x) = -\frac{1}{3}(x + 2)(x - 3)$.

28. C

The coordinates of the vertex are $(-2, 6)$.

The equation is in the form $y = a(x + 2)^2 + 6$, where a is a constant.

The answer is C.

29. A

I. ✓. Coefficient of $x^2 = 1 > 0$.

II. ✗. y -intercept $= m^2 + n$.

Take $m = 0$ and $n = -1$, then the y -intercept is not positive.

III. ✗. When $x = n$, $y = (m - n)^2 + n \geq n$.

Take $m = -1$ and $n = 1$, then $y \neq m$ obviously.

30. C

$(3, -4)$ lies on $y = f(x) \Rightarrow f(3) = -4$

$$f(x) + 4 = 0$$

$$f(x) = -4$$

$$x = 3$$

(vertex $\rightarrow 3$ is a repeated root)

The roots of the equation $f(x) + 4 = 0$ are real numbers.

Conventional Questions

31. (a) $0 = -x^2 + 7x - 6$
 $x = 1$ or 6
 Coordinates of A and B are $(1, 0)$ and $(6, 0)$ respectively. 1A+1A
 Coordinates of C are $(0, -6)$. 1A
- (b) $y = -x^2 + 7x - 6$

$$= -\left[x^2 - 2\left(\frac{7}{2}\right)x + \left(\frac{7}{2}\right)^2\right] + \frac{25}{4}$$
 1M

$$= -\left(x - \frac{7}{2}\right)^2 + \frac{25}{4}$$

 Thus, coordinates of P are $\left(\frac{7}{2}, \frac{25}{4}\right)$. 1A
 Equation of L is $y = \frac{25}{4}$. 1A
32. (a) Substitute $x = 8$ into $2x - y - 1 = 0$, we have $y = 6$.
 The coordinates of C are $(8, 6)$ and therefore $k = 6$. 1A
 Substitute $y = 0$ into $2x - y - 10 = 0$, we have $x = 5$.
 The coordinates of A are $(5, 0)$. 1A
 Substitute $(5, 0)$ into $y = a(x - 8)^2 + 6$,

$$0 = a(5 - 8)^2 + 6$$
 1M

$$a = -\frac{2}{3}$$
 1A
- (b) When $y = 0$,

$$0 = -\frac{2}{3}(x - 8)^2 + 6$$
 1M
 $x = 11$ or 5
 The coordinates of B are $(11, 0)$. 1A
 Slope of $BC = \frac{6 - 0}{8 - 11} = -2$.
 The equation of BC is

$$y - 6 = -2(x - 8)$$
 1M

$$y = -2x + 22$$
 1A
33. (a) Since the coordinates of the vertex of the graph are $(3, 8)$ and the graph intersects the x -axis at two points,
 $(3, 8)$ is the maximum point of the graph of $y = f(x)$. 1M
 Thus, the graph of $y = f(x)$ opens downwards. 1A
- (b) By (a), $f(x) \leq 8$.
 Thus, $k > 8$. 1A

- (c) The axis of symmetry is $x = 3$. 1A
 One of the x -intercept is 1. 1A
 Let the other x -intercept be β .

$$\frac{1 + \beta}{2} = 3$$
 1M

$$\beta = 5$$

 The two x -intercepts are 1 and 5. 1A
34. (a) $3 = -3^2 + 8(3) + k$ 1M
 $k = -12$ 1A
- (b) $0 = -x^2 + 8x - 12$
 $x = 2$ or 6
 The coordinates of A and B are $(2, 0)$ and $(6, 0)$ respectively. 1A+1A
- (c) (i) x -coordinate of mid-point of $AB = \frac{2+6}{2} = 4$.
 The axis of symmetry is $x = 4$. 1A
- (ii) $CP : PB = (4 - 3) : (6 - 4)$ 1M
 $= 1 : 2$ 1A