REV-PROB-2324-ASM-SET 1-MATH

Suggested solutions

Multiple Choice Questions

- 1. C
- 2. C
- 3. A
- 4. B
- 5. C

- 6. C
- 7. D
- 8. C
- 9. A
- 10. D

- 11. C
- 12. D
- 13. D
- 14. B
- 15. C

- 16. D
- 17. B
- 18. B
- 19. D
- 20. D

- 21. B
- 22. C
- 23. A
- 24. B
- 25. B

- 26. D
- 27. C
- 28. C
- 29. D
- 30. B

1. **C**

Required probability =
$$1 - 0.8^5$$

$$= 0.67232$$

2. **C**

It is possible that the sum of two numbers is 6 and the 2 numbers are both odd.

We have $P(A \cap B) > 0$.

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$< P(A) + P(B)$$

3. A

Number of students taking both subjects = 16 + 21 - 30 = 7

Required probability =
$$\frac{7}{30}$$

4. B

Required probability =
$$1 - \frac{C_2^5 + C_2^8}{C_2^{14}} = \frac{53}{91}$$

5. **C**

Required probability =
$$\frac{\left(\frac{1}{36}\right)}{1 - \left(\frac{5}{6}\right)^2}$$
$$= \frac{1}{11}$$

Required probability = $1 - 0.7^4 = 0.7599$

7. D

Required probability = 1 - P(same colour)

$$=1 - \left(\frac{(2)(3) + (5)(4)}{(11)(10)}\right) = \frac{42}{55}$$

8. **C**

Required probability =
$$1 - \frac{20}{30} \times \frac{15}{30}$$

= $\frac{2}{3}$

Required probability =
$$1 - \left(\frac{3}{4}\right)^3$$

= $\frac{37}{64}$

Required probability =
$$\frac{5}{7} \times \frac{5}{7}$$

= $\frac{25}{49}$

Required probability =
$$1 - 0.7^3 - (1 - 0.7)^3$$

= 0.63

Required probability =
$$\frac{3}{7} \times \frac{2}{7} + \frac{4}{7} \times \frac{5}{7}$$

= $\frac{26}{49}$

Required probability =
$$C_2^3 \left(\frac{2}{5}\right)^2 \left(\frac{3}{5}\right) = \frac{36}{125}$$

Required probability =
$$1 - \frac{1}{4} - \frac{1}{12} - \frac{1}{24} - \frac{1}{48}$$

= $\frac{29}{48}$

Required probability =
$$\frac{2}{5} \times \frac{5}{6} + \frac{3}{5} \times \frac{4}{6}$$

= $\frac{11}{15}$

16. D

Required probability =
$$\frac{\left(\frac{C_2^3}{C_2^8}\right)}{1 - \frac{C_2^5}{C_2^8}}$$
$$= \frac{1}{6}$$

17. B

Required probability =
$$\frac{1}{8} + \frac{1}{8} - \frac{6!}{8!}$$

= $\frac{13}{56}$

18. B

Required probability =
$$\frac{3+6}{36}$$

= $\frac{1}{4}$

19. D

Required probability =
$$\frac{1}{2} \times \frac{4}{2+4} + \frac{1}{2} \times \frac{3}{1+3} = \frac{17}{24}$$

20. D

Needs at least 3 draws \Leftrightarrow no gold coins obtained in first 2 draws Required probability = $\frac{C_2^3}{C_2^7} = \frac{1}{7}$

21. B

Required probability =
$$\frac{10}{20} + \frac{4}{20} - \frac{2}{20}$$

= $\frac{3}{5}$

22. **C**

Required probability =
$$\frac{3}{10} + \frac{2}{10} - \frac{1}{10}$$

= $\frac{2}{5}$

23. A

Required probability =
$$1 - \frac{1}{4} - \frac{1}{5} - \frac{1}{6}$$

= $\frac{23}{60}$

24. B

Required probability =
$$\frac{2}{5} \times \frac{1}{6}$$

= $\frac{1}{15}$

25. B

Required probability =
$$\frac{5}{8} \times \frac{5}{8} + \frac{3}{8} \times \frac{1}{4} = \frac{31}{64}$$

26. D

Required probability =
$$1 - \frac{C_4^4}{C_4^6} = \frac{14}{15}$$

27. **C**

Probability of getting a green ball =
$$\frac{1}{3} \times \frac{1}{7} + \frac{1}{3} \times \frac{2}{7} + \frac{1}{3} \times \frac{3}{7} = \frac{2}{7}$$

Required probability = $\frac{\frac{1}{3} \times \frac{1}{7}}{\frac{2}{7}} = \frac{1}{6}$

28. **C**

Probability of Ivan and Jason sit next to each other in the 2nd row =
$$\frac{2 \times 2! \times 7!}{9!} = \frac{1}{18}$$

Required probability = $\frac{\left(\frac{1}{18}\right)}{\left(\frac{3}{9}\right)} = \frac{1}{6}$

29. D

Required probability =
$$1 - \frac{1}{3} \times \frac{1}{5} \times \frac{1}{7} = \frac{104}{105}$$

30. B

Required probability =
$$1 - 0.2 - 0.25$$

= 0.55