REV-EOSL-2324-ASM-SET 1-MATH

Suggested solutions

Multiple Choice Questions

1. D

2. D

3. A

4. D

5. A

6. C

7. D

8. C

9. C

10. C

11. B

12. A

13. D

14. C

15. C

16. A

17. B

18. B

19. B

20. B

21. C

22. D

23. D

24. A

25. A

26. D

27. A

28. A

29. D

30. B

1. D

5(6) - 8y - 14 = 0 and 5x - 8(-3) - 14 = 0

$$y = 2$$

$$x = -2$$

The coordinates of A and C are (-2, -3) and (6, 2) respectively.

Required area = (6+2)(2+3)

$$= 40 \text{ sq. units}$$

2. D

Let A(a, 1) and B(2, b). Substitute them into y = 2x + 3, we have a = -1 and b = 7. Distance between A and $B = \sqrt{(2+1)^2 + (7-1)^2} = \sqrt{45} = 3\sqrt{5}$

3. A

Slope required line = $\frac{-1}{2}$ Required equations is

$$y = \frac{-1}{2}x$$

$$x + 2y = 0$$

4. D

Slope of
$$L_1 = \tan 30^\circ = \frac{1}{\sqrt{3}}$$

Slope of
$$L_2 = -\sqrt{3}$$

Equation of L_2 is

$$y = -\sqrt{3}x$$

$$\sqrt{3}x + y = 0$$

5. A

Slope of
$$L_1 = \frac{4-0}{-1-0} = -4$$

Slope of
$$L_2 = \frac{1}{4}$$

Required equation is

$$y - 4 = \frac{1}{4}(x+1)$$

$$x - 4y + 17 = 0$$

6. <u>C</u>

Let the x-intercept be a. Then the y-intercept is also a.

Slope of the line =
$$\frac{a-0}{0-a} = -1$$

Required equation is

$$y - 5 = -1(x - 3)$$

$$x + y - 8 = 0$$

7. D

The coordinates of the mid-point of AB are $\left(-1, \frac{11}{2}\right)$.

Slope of
$$AB = \frac{8-3}{-4-2} = -\frac{5}{6}$$

Required equation is

$$y - \frac{11}{2} = \frac{6}{5}(x+1)$$

$$12x - 10y + 67 = 0$$

8. C

Slope of
$$L_1 = -\tan 30^{\circ} = -\frac{1}{\sqrt{3}}$$

Slope of
$$L_2 = \sqrt{3}$$

Required equation is

$$y - 0 = \sqrt{3}(x+1)$$

$$\sqrt{3}x - y + \sqrt{3} = 0$$

9. **C**

Slope of
$$L = -\tan 45^\circ = -1$$

Required equation is

$$y - 0 = -1(x + 3)$$

$$x + y + 3 = 0$$

10. **C**

The coordinates of mid-point of BD are (4, 6).

Slope of
$$BD = \frac{9-3}{5-3} = 3$$

Required equation is

$$y - 6 = -\frac{1}{3}(x - 4)$$

$$x + 3y - 22 = 0$$

11. **B**

Since OA = AB, we have $\angle AOB = \angle ABO$ and slope of OA is -m.

Required equation is

$$y = -mx$$

$$mx + y = 0$$

12. A

mid-point of *BC* is at (7, 5). Required straight line passes through *A* and (7, 5). Slope of the line $=\frac{5-3}{7-3}=\frac{1}{2}$.

Slope of the line =
$$\frac{5-3}{7-3} = \frac{1}{2}$$

Only the line in option A has slope $\frac{1}{2}$.

13. D

Slope =
$$\frac{7-3}{0+2} = 2$$

Required equation is

$$y - 7 = 2(x - 0)$$

$$y = 2x + 7$$

14. **C**

Slope =
$$\frac{4+7}{-6+2} = -\frac{11}{4}$$

$$y - 4 = -\frac{11}{4}(x+6)$$

$$11x + 4y + 50 = 0$$

15. C

Let the coordinates of P be (p, 0).

$$\frac{-3-0}{3-p} = \frac{1+3}{7-3}$$

$$p = 6$$

Slope of required line = $\frac{3-0}{0-6} = -\frac{1}{2}$ Required equation is

$$y - 3 = -\frac{1}{2}(x - 0)$$

$$x + 2y - 6 = 0$$

16. A

Let the coordinates of P be (p, p) such that P lies on the straight line x = y.

$$AP = PB$$

$$\sqrt{(p-2)^2 + (p-5)^2} = \sqrt{(p-6)^2 + (p+3)^2}$$

$$2p^2 - 14p + 29 = 2p^2 - 6p + 45$$

$$p = -2$$

The coordinates of P are (-2, -2).

17. B

Let the coordinates of P be (p, p + 1) such that P lies on y = x + 1.

$$AP = PB$$

$$\sqrt{(p-3)^2 + (p+1-9)^2} = \sqrt{(p-7)^2 + (p+1-1)^2}$$

$$2p^2 - 22p + 73 = 2p^2 - 14p + 49$$

$$p = 3$$

The coordinates of P are (3, 4).

18. B

Let the coordinates of C be (2c, c) such that it lies on x - 2y = 0.

$$\sqrt{(9-2c)^2 + (-2-c)^2} = \sqrt{(-1-2c)^2 + (8-c)^2}$$
$$-20c + 20 = 0$$
$$c = 1$$

The x-coordinate of C is 2.

19. B

$$A(0, 2)$$
 and $B(-6, 0)$.
Area = $\frac{(2)(6)}{2} = 6$

20. B

Required equation is in the form 3x + 4y + k = 0, where k is a constant. The answer is B.

21. C

$$5(0) - 8y - 40 = 0$$
 and $5x - 8(0) - 40 = 0$
 $y = -5$ $x = 8$

The coordinates of A and B are (8, 0) and (0, -5) respectively.

The coordinates of M are (4, 0).

Slope of
$$L_2 = \frac{0+5}{4-0} = \frac{5}{4}$$

Required equation is

$$y + 5 = \frac{5}{4}(x - 0)$$

$$5x - 4y - 20 = 0$$

The slopes of the lines are $-\frac{1}{3}$ and $\frac{k}{3}$ respectively.

$$-\frac{1}{3} \times \frac{k}{3} = -1$$
$$k = 9$$

$$\frac{x}{2} + \frac{y}{3} = 1$$
$$y = -\frac{3x}{2} + 3$$

Slope of required line is $\frac{2}{3}$.

The answer is D.

$$L_1: y = -\frac{3x}{2} + \frac{3}{4} \implies \text{slope} = -\frac{3}{2}$$

$$L_2: y = -\frac{3x}{2} + 4 \implies \text{slope} = -\frac{3}{2}$$

$$L_3: y = \frac{3x}{2} + \frac{3}{4} \implies \text{slope} = \frac{3}{2}$$

I. ✓. Equal slopes.

II. X. Different slopes.

III. **X**. Product of slope
$$= -\frac{3}{2} \times \frac{3}{2} = -\frac{9}{4} \neq -1$$

$$\frac{-3}{2} \times \frac{-k}{12} = -1$$

$$k = -8$$

$$\frac{-k}{4} \times \frac{6}{9} = -1$$

$$k = 6$$

L: 6x + 4y - 12 = 0. The y-intercept is 3.

27. A

Slope of the line =
$$\frac{9}{5}$$

Slope of
$$L = -\frac{5}{9}$$

Equation of L is

$$y - 3 = -\frac{5}{9}(x+3)$$

$$5x + 9y + 15 = 0$$

Required equation is in the form 3x - 5y + C = 0, where C is a constant.

$$3(k) - 5(-k) + C = 0$$

$$C = -8k$$

Required equation is 4x - 5y - 8k = 0.

29. D

Slope of
$$x + 2y + 3 = 0$$
 is $-\frac{1}{2}$.

Required equation is

$$y - 3 = 2(x - 1)$$

$$2x - y + 1 = 0$$

Take
$$a = b = 1$$
 and $c = -1$.

$$ax + by + c = 0$$

$$x + y - 1 = 0$$

$$y = -x + 1$$

The graph is a straight line with slope -1 and y-intercept 1.

The answer is B.