REV-FG-2324-ASM-SET 1-MATH

Suggested solutions

Multiple Choice Questions

- 1. A
- 2. C
- 3. C
- 4. D
- 5. D

- 6. C
- 7. C
- 8. A
- 9. B
- 10. A

- 11. A
- 12. D
- 13. A
- 14. C
- 15. B

- 16. C
- 17. D
- 18. C
- 19. C
- 20. B

- 21. D
- 22. A
- 23. C
- 24. A
- 25. C

- 26. C
- 27. B
- 28. C
- 29. D
- 30. D

1. A

Function parts	Related restrictions	Conclusion
Square root	Non-negative real numbers	$x-4 \ge 0$
Fraction	Denominator ≠ 0	$\sqrt{x-4} \neq 0$

We have x > 4.

2. **C**

Function of $x \implies$ for each value of x, there is **only one** value of y.

For each vertical line (same x), there is only one intersection with the graph (one value of y). The answer is C.

$$3f(2) - 1 = 3[2^2 - 3(2) + 17] - 1$$

= 44

$$f(x) - f\left(\frac{1}{x}\right) = \left(x - \frac{1}{x}\right) - \left(\frac{1}{x} - x\right)$$
$$= 2\left(x - \frac{1}{x}\right)$$

$$f(x-1) = 2(x-1)^2 + 1$$
$$= 2x^2 - 4x + 3$$

6. C

$$f(c) + f(-c) = [(c)^{3} + (-c)^{3}] + c[(c)^{2} + (-c)^{2}] + [c + c]$$
$$= c(2c^{2}) + (2c)$$
$$= 2c^{3} + 2c$$

7. **C**

$$f(x+1) - f(x) = [(x+1)^2 - (x)^2] - [(x+1) - (x)] + [1-1]$$
$$= (2x+1) - 1$$
$$= 2x$$

8. A

$$f(5) - f(3) = [5^2 - 3^2] + 2[5 - 3] + [k - k]$$
$$= 16 + 4$$
$$= 20$$

9. B

$$f(2) \cdot f(-2) = (a+2b)(a-2b)$$
$$= a^2 - 4b^2$$

10. A

$$\begin{cases} f(0) = 1 = h(-3) + k \\ f(8) = 1 = (8 + h)(5) + k \end{cases}$$
 Solving, we have $h = -5$ and $k = -14$.

11. A

$$f(1) = f(-1)$$

$$\frac{a}{1} + b + c(1) + d(1)^{2} = \frac{a}{-1} + b + c(-1) + d(-1)^{2}$$

$$2a + 2c = 0$$

$$a + c = 0$$

12. D

$$g(-1) = g(7)$$

$$(-1)^{2} - 2k(-1) + 1 = (7)^{2} - 2k(7) + 1$$

$$2 + 2k = 50 - 14k$$

$$k = 3$$

13. A

$$f(2) = f(1) - 1$$
$$2^{2} + 2a(2) - 12 = (1 + 2a - 12) - 1$$
$$a = -2$$

14. **C**

$$f(4) - f(3) = 21$$
$$[4^{2} - 3^{2}] + k[4 - 3] + [7 - 7] = 21$$
$$7 + k = 21$$
$$k = 14$$

15. B

$$f(x) = g(x)$$

$$5 + 2x = x^{2} - x - 5$$

$$0 = x^{2} - 3x - 10$$

$$x = 5 \quad \text{or} \quad -2$$

16. **C**

Sign	Graph	Conclusion
<i>a</i> < 0	open downwards	
<i>b</i> > 0	slope at y-intercept is positive	A 🗸 and B 🔏
c < 0	y-intercept is negative	ac > 0 and D X

The answer is C.

17. D

Graph	Conclusion
Open downwards	<i>a</i> < 0
y-intercept > 0	b > 0

The answer is D.

18. **C**

Graph	Conclusion
Open upwards	m > 0
y-intercept < 0	n < 0

The answer is C.

19. **C**

Graph	Conclusion
Open downwards	m < 0
y-intercept > 0	<i>n</i> > 0

The answer is C.

20. B

We have c = 5.

Let the other *x*-intercept be β .

Then 1 and β are roots of $x^2 + bx + 5 = 0$.

Product of roots = $1\beta = \frac{5}{1}$

$$\beta = 5$$

Equation of axis of symmetry is

$$x = \frac{1+5}{2}$$

$$x = 3$$

21. D

Coordinates of vertex are (-1, 1).

Vertex of the graph lies in the second quadrant.

$$y\text{-intercept} = -2(0+1)^2 + 1$$

$$= -1 < 0$$

The answer is D.

22. A

Axis of symmetry is x = -5.

23. **C**

$$y = (px + 5)^2 + q$$

$$= p^2 \left(x + \frac{5}{p} \right)^2 + q$$

Coordinates of vertex are $\left(-\frac{5}{p}, q\right)$.

Vertex $\left(-\frac{5}{p}, q\right)$ lies in quadrant III, we have $\frac{-5}{p} < 0$ and q < 0. Thus, p > 0 and q < 0.

24. A

Coordinates of vertex are (-h, k).

$$-h < 0$$
 and $k > 0$

25. C

Coordinates of V are (5, -9).

$$0 = (x - 5)^2 - 9$$

$$x - 5 = \pm \sqrt{9}$$

$$x = 2$$
 or 8

Coordinates of A and B are (2, 0) and (8, 0) respectively.

Required area =
$$\frac{(8-2)(9)}{2}$$

$$= 27$$

26. C

Coordinates of vertex are (1, 1).

Vertex of the graph lies in the first quadrant.

The answer is C.

27. B

Coordinates of vertex are (-h, k).

$$-h < 0$$
 and $k < 0$

The answer is B.

28. **C**

Coordinates of vertex are (h, -1).

$$8 = (0 - h)^2 - 1$$

$$h = -3$$
 or 3 (rejected)

Axis of symmetry is x = -3.

29. D

y-intercept =
$$(0+2)^2 - 1$$

$$= 3 \neq -1$$

The answer is D.

30. D

A. **X**. y-intercept =
$$29 - (0 - 2)^2 = 25$$

B. **X**. When
$$x = -3$$
, $y = 29 - (-3 - 2)^2 = 4 \neq 22$.

D.
$$\checkmark$$
. $0 = 29 - (x - 2)^2$

$$x = 2 \pm \sqrt{29}$$