### **REG-EXP-2223-ASM-SET 2-MATH**

## **Suggested solutions**

### **Multiple Choice Questions**

1. C

2. B

3. A

4. D

5. C

6. A

7. C

8. A

9. C

10. A

11. A

12. A

13. B

14. C

15. A

16. B

17. C

18. C

19. C

20. D

21. A

22. C

23. A

24. A

25. C

26. C

27. D

28. B

29. A

30. C

1. **C** 

$$27^x = (3^x)^3$$

$$= a^3$$

2. B

$$a^{2} + \frac{1}{a} = b + \frac{1}{\sqrt{b}}$$

$$= b + \frac{\sqrt{b}}{b}$$

$$= \frac{b^{2} + \sqrt{b}}{b}$$

3. A

$$x^{-\frac{3}{2}} = \frac{1}{8}$$
$$x = \left(\frac{1}{8}\right)^{-\frac{2}{3}}$$

4. D

$$5^{3x+4} \cdot 5^{\frac{1}{2}} = 125$$
$$5^{3x+4+\frac{1}{2}} = 5^3$$

$$3x + \frac{9}{2} = 3$$

$$x = -\frac{1}{2}$$

$$(2^{x})(16^{y}) = (\sqrt{8})^{z}$$
$$(2^{x})(2^{4y}) = 2^{\frac{3z}{2}}$$
$$x + 4y = \frac{3z}{2}$$

$$x + 4y = \frac{32}{2}$$
$$z = \frac{2}{3}(x + 4y)$$

$$\frac{64^x \cdot 4^{-2y}}{2^{3x}} = 1$$

$$2^{6x} \cdot 2^{-4y} = 2^{3x}$$

$$6x - 4y = 3x$$

$$\frac{x}{y} = \frac{4}{3}$$

$$16^x = \frac{1}{\sqrt{8}}$$

$$2^{4x} = 2^{-\frac{3}{2}}$$

$$4x = -\frac{3}{2}$$
$$x = -\frac{3}{8}$$

$$x = -\frac{3}{8}$$

# 8. A

$$(2^x)(4^x)(8^x) = 16$$

$$2^{x+2x+3x} = 2^4$$

$$6x=4$$

$$x = \frac{2}{3}$$

$$3^{x+2y} = 1$$
 and  $4^x \cdot 8^y = 2$ 

$$x + 2y = 0 2^{2x + 3y} = 2^1$$

$$2x + 3y = 1$$

Solving, we have x = 2 and y = -1.

# 10. A

$$4^{x+2y} = 2$$
 and  $3^{x+y} = 1$ 

$$2^{2x+4y} = 2^1 \qquad x + y = 0$$

$$2x + 4y = 1$$

Solving, we have  $x = -\frac{1}{2}$  and  $y = \frac{1}{2}$ .

$$2^{x+3y} = 32$$
 and  $2^{3x+y} = \frac{1}{2}$ 

$$x + 3y = 5 \qquad 3x + y = -1$$

Solving, we have x = -1 and y = 2.

Thus, x + y = 1.

$$8^{x+\frac{1}{3}} + 8^{x-\frac{1}{3}} = 20$$

$$8^x(8^{\frac{1}{3}} + 8^{-\frac{1}{3}}) = 20$$

$$8^{x} = 8$$

$$x = 1$$

$$49^{x+1} = 7^{2x-1} + 342$$

$$7^{2x+2} - 7^{2x-1} = 342$$

$$7^{2x}(7^2 - 7^{-1}) = 342$$

$$7^{2x} = 7$$

$$2x = 1$$

$$x = \frac{1}{2}$$

$$3^x = 36 - 3^{x-1}$$

$$3^x(1+3^{-1}) = 36$$

$$3^x = 27$$

$$x = 3$$

$$7^x + 7^{x+1} = 392$$

$$7^x(1+7) = 392$$

$$7^x = 49$$

$$x = 2$$

$$2^{2x+2} - 3(2^{2x}) = 128$$

$$2^{2x}(2^2 - 3) = 128$$

$$2^{2x} = 128$$

$$2^{2x} = 2^7$$

$$2x = 7$$

$$x = \frac{7}{2}$$

$$2^{2x+3} - 4^{x+1} = 128$$

$$2^{2x+3} - 2^{2x+2} = 128$$

$$2^{2x}(2^3 - 2^2) = 128$$

$$2^{2x} = 32$$

$$2^{2x} = 2^5$$

$$2x = 5$$

$$x = \frac{5}{2}$$

$$4^{x} = 3(4^{x-1}) + 16$$

$$4^{x} - \frac{3}{4} \cdot 4^{x} = 16$$

$$4^{x} \left(1 - \frac{3}{4}\right) = 16$$

$$4^{x} = 64$$

$$x = 3$$

Required number = 
$$40(1.4)^3$$
  
  $\approx 110$ 

$$4000000 = A(1.08)^{0}$$

$$A = 4000000$$
Required value =  $A(1.08)^{2}$ 
= \$4665600

21. A

For the graph of  $y = \left(\frac{1}{3}\right)^{-x}$ .

x	-1	0	1
у	$\frac{1}{3}$	1	3

The graph passes through  $\left(-1, \frac{1}{3}\right)$ , (0, 1) and (1, 3).

The answer is A.

22. **C** 

The graph passes through (-1, 4) and (0, 1).

A. **X**. The graph of  $y = 4^x$  does not pass through (-1, 4).

B. **X**. The graph of  $y = -4^x$  does not pass through (0, 1).

C. 🗸

D. **X**. The graph of  $y = -\left(\frac{1}{4}\right)^x$  does not pass through (0, 1).

23. A

For the graph of  $y = 2^x$ .

x	-1	0	1
у	$\frac{1}{2}$	1	2

The graph passes through  $\left(-1, \frac{1}{2}\right)$ , (0, 1) and (1, 2).

The answer is A.

24. A

$$a = 3^0 = 1$$

$$b = 3^a = 3^1 = 3$$

25. C

$$2=ka^0$$

$$k = 2$$

26. **C** 

The line x = 1 intersects the graph of  $y = 2^x$  and  $y = 3^x$  at (1, 2) and (1, 3) respectively.

The answer is therefore C.

27. D

The line x = 1 intersects the graph of  $y = 2^x$  and the graph of  $y = \left(\frac{3}{2}\right)^x$  at (1, 2) and  $\left(1, \frac{3}{2}\right)$  respectively.

Since the y-intercept is 1, the intersection of the required curve and x = 1 should lie above the y-intercept.

The answer is D.

28. B

Required graph is  $y = 5^{-(-x)} = 5^x$ .

29. A

$$a^x = b^{-x}$$

$$a^x b^x = 1$$

$$(ab)^x = 1$$

ab = 1

30. C

Draw the line y = 10.

We have x = 1.4.

#### **Conventional Questions**

31. 
$$3^{x} + 3^{x+1} = 108$$
  
 $3^{x}(1+3) = 108$   
 $3^{x} = 27$   
 $3^{x} = 3^{3}$   
 $x = 3$   
1M

32. 
$$2^{2x+1} + 3(4^x) - 2^{2x-1} = 36$$
  
 $2^{2x}(2+3-2^{-1}) = 36$   
 $2^{2x} = 8$   
 $2x = 3$   
 $x = \frac{3}{2}$   
1A

33. (a) 
$$P(1.32)^0 = 20$$
 1M
$$P = 20$$
 1A
(b) Required number =  $20(1.32)^5$  1M
$$\approx 80$$
 1A
(c) Ratio of number of bananas =  $\frac{P(1.32)^{2t}}{P(1.32)^t}$  1M
Since  $t$  may not be equal to 2, the ratio may not equal  $1.32^2$ .

Since t may not be equal to 2, the ratio may not equal  $1.32^2$ .

The claim is disagreed.

34. (a) Required cost = 
$$45\,000(20)^{-0.2}$$
 1M  $\approx $24\,700$  1A (b) Required percentage decrease =  $\frac{45\,000(5)^{-0.2} - 45\,000(20)^{-0.2}}{45\,000(5)^{-0.2}} \times 100\%$  1M  $\approx 24.2\%$  1A

35. (a) Suppose Wilkins and Sally meet after r hours from 10:00.

$$\frac{30 - 10.5}{r} = \frac{30 - 4}{4}$$

$$r = 3$$

Wilkins and Sally will meet at 13:00.

1**A** 

(b) When t = 0, x = 0,

$$0 = \frac{3}{2}(a^0 - k)$$

$$0 = 1 - k$$

$$k = 1$$

When t = 3, x = 10.5,

$$10.5 = \frac{3}{2}(a^3 - 1)$$
$$a^3 = 8$$

$$a^{2} = 8$$

$$a^3 = 2^3$$

1M

a = 2

(c) When 
$$t = 4$$
,

$$x = \frac{3}{2}(2^4 - 1)$$
$$= 22.5$$

1A

Distance between Sally and town 
$$M$$
 at  $14:00 = \left[30 - (1)\left(\frac{30 - 4}{4}\right)\right]$  km =  $23.5$  km  $> 22.5$  km

1M

She cannot meet Wilkins before 14:00.

1A